

ECE 465, Fall 2009
Homework 3

1. Prob. 3.63 using the alternate to Rule 6 followed by the sweep-up phase.

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Solution:

$$f_a(A,B,C,D,E) = \sum m(0,4,6,20,22) + d(2,10,18)$$

$$f_b(A,B,C,D,E) = \sum m(4,6,11,19,20,27) + d(18,22)$$

Min-term	List 1 ABCDE	Flags	Min-terms	List 2 ABCDE	Flags	Min-terms	List 3 ABCDE	Flags
0	00000	α ✓	0,2	000-0	α ✓	0,2,4,6	00- -0	α PI_1
2	00010	α ✓	0,4	00-00	α ✓	2,6,18,22	-0-10	α PI_2
4	00100	$\alpha\beta$ ✓	2,6	00-10	α ✓	4,6,20,22	-01-0	$\alpha\beta$ PI_3
6	00110	$\alpha\beta$ ✓	2,10	0-010	α PI_4			
10	01010	α ✓	2,18	-0010	α ✓			
18	10010	$\alpha\beta$ ✓	4,6	001-0	$\alpha\beta$ ✓			
20	10100	$\alpha\beta$ ✓	4,20	-0100	$\alpha\beta$ ✓			
11	01011	β ✓	6,22	-0110	$\alpha\beta$ ✓			
19	10011	β ✓	18,19	1001-	β PI_5			
22	10110	$\alpha\beta$ ✓	18,22	10-10	$\alpha\beta$ PI_6			
27	11011	β ✓	20,22	101-0	$\alpha\beta$ ✓			
			11,27	-1011	β PI_7			
			19,27	1-011	β PI_8			

		f_a					f_b					
		✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	
		0	4	6	20	22	4	6	11	19	20	27
$\ast PI_1$	α	⊗	x	x								
PI_2	α			x	x							
$\ast PI_3$	$\alpha\beta$		x	x	⊗	x	⊗	⊗			⊗	
PI_4	α											
PI_5	β									x		
PI_6	$\alpha\beta$					X						
$\ast PI_7$	β								⊗			x
PI_8	β									x		x

Essential prime implicants: PI_1 and PI_3 for function f_a ; PI_3 and PI_7 for f_b .

All minterms of f_a are covered. Choose PI_5 or PI_8 to cover minterm 19 of f_b

$$f_a = PI_1 + PI_3 = \bar{A}\bar{B}\bar{E} + \bar{B}C\bar{E}$$

$$f_b = PI_3 + PI_7 + PI_8 = \bar{B}C\bar{E} + \bar{B}CDE + A\bar{B}C\bar{D}$$

or

$$f_b = PI_3 + PI_7 + PI_8 = \bar{B}C\bar{E} + \bar{B}CDE + A\bar{C}DE$$

The above is the solution obtained before the sweep-up phase. The EPIs and pseudo-EPIs are:

PI_1 and PI_3 in f_a (these are all f_a 's PIs) and PI_3 and PI_7 in f_b . Deleting the MTs covered By PI_3 and PI_7 in f_b , we get MT 19 remaining which need to be covered by PI_5 or PI_8 . Both have the same cost, so either choice is OK, and the solution remain unchanged after sweep-up.

4. Implement a 2-bit adder function (i.e., a 2-bit binary number a_1a_0 added to another 2-bit binary number b_1b_0 to yield a 3-bit sum $s_2s_1s_0$) using three 8:1 MUXes. Derive the TT and show all steps clearly for deriving the (data) inputs to the MUXes. 40

Solution:

2-bit adder

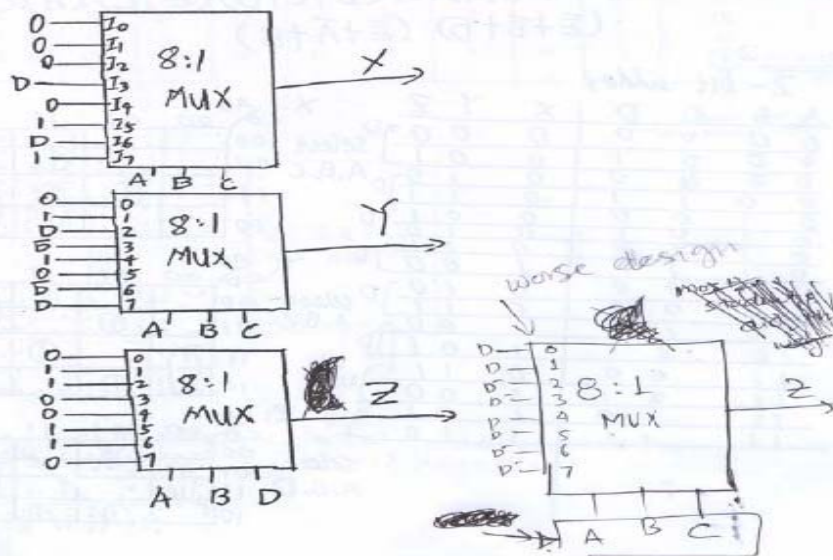
A	B	C	D	X	Y	Z
0	0	0	0	0	0	0
0	0	0	1	0	0	1
0	0	1	0	0	1	0
0	0	1	1	0	1	1
0	1	0	0	0	0	1
0	1	0	1	0	1	1
0	1	1	0	1	0	0
0	1	1	1	1	0	1
1	0	0	0	0	1	0
1	0	0	1	0	1	1
1	0	1	0	1	0	0
1	0	1	1	1	0	1
1	1	0	0	0	1	1
1	1	0	1	1	0	0
1	1	1	0	1	0	1
1	1	1	1	1	1	0

CD	00	01	11	10
00	0	0	0	0
01	0	0	1	0
11	0	1	0	0
10	0	1	1	0

CD	00	01	11	10
00	0	0	0	0
01	0	0	1	0
11	0	1	0	0
10	0	1	1	0

CD	00	01	11	10
00	0	0	0	0
01	0	0	1	0
11	0	1	0	0
10	0	1	1	0

$$\begin{aligned}
 X &= (\bar{A}\bar{B}C) \cdot 0 + (\bar{A}B\bar{C}) \cdot 0 + (\bar{A}BC) \cdot 0 + (\bar{A}BC) \cdot D + (A\bar{B}\bar{C}) \cdot 0 \\
 &\quad + (A\bar{B}C) \cdot 1 + (AB\bar{C}) \cdot D + (ABC) \cdot 1 \\
 Y &= (\bar{A}\bar{B}\bar{C}) \cdot 0 + (\bar{A}\bar{B}C) \cdot 1 + (\bar{A}B\bar{C}) \cdot D + (\bar{A}BC) \cdot \bar{D} + (A\bar{B}\bar{C}) \cdot 1 \\
 &\quad + (A\bar{B}C) \cdot 0 + (AB\bar{C}) \cdot \bar{D} + (ABC) \cdot D \\
 Z &= (\bar{A}\bar{B}\bar{D}) \cdot 0 + (\bar{A}\bar{B}D) \cdot 1 + (\bar{A}B\bar{D}) \cdot 1 + (\bar{A}BD) \cdot 0 + (A\bar{B}\bar{D}) \cdot 0 \\
 &\quad + (A\bar{B}D) \cdot 1 + (AB\bar{D}) \cdot 1 + (ABD) \cdot 0
 \end{aligned}$$



5. Implement the function $f(A, B, C, D) = \sum m(2, 4, 5, 8, 10, 12, 13, 14)$ using a 4:1 MUX and a choice of 2 control variables such that a minimal number of 2-i/p AND/OR gates are used. Assume that the inverted inputs of all variables are available for free. 50

Solution:

